(06 Marks)

2. Any eyealing of identification, appeal to evaluator and /or equations written eg, 42+8 = 50, will be treated as malpractice. Important Note: 1. On completing your answers, compulsorily draw diagonal cross lines on the remaining blank pages.

for the message.

Fourth Semester B.E. Degree Examination, Dec.2014/Jan.2015 Graph Theory and Combinatorics

Max. Marks: 100 Time: 3 hrs. Note: Answer any FIVE full questions, selecting atleast TWO questions from each part. PART - A Define graph isomorphism and isomorphic graphs. Determine whether the following graphs (05 Marks) are isomorphic or not: Fig.Q.1(a) b. Define complement of a simple graph. Let G be a simple graph of order n. If the size of G is (05 Marks) 56 and the size of \overline{G} 180. What is n? c. Let G = (V, E) be a connected undirected graph. What is the largest possible value for |V| if (04 Marks) |E| = 19 and $deg(v) \ge 4$ for any $\in V$? d. Write a note on "Konigsberg bridge problem and its solution". (06 Marks) esen graph is nonplanar. (05 Marks) Define planar graph. Prove that the 2 a. Define Hamilton cycle. How many edge disjoint Hamilton cycles exist in the complete graph with seven vertices? Also draw the graph to show these Hamilton cycles. (05 Marks) Define dual of a planar graph construct the dual of the planar graph given in Fig.Q.2(c). (04 Marks) Fig.Q.2(c)number and chromatic polynomial. Determine the chromatic polynomial Define chromatic (06 Marks) for the graph how in Fig.Q.2(d). Fig.Q.2(d) class room contains 10 micro computer that are to be connected to a wall socket that has 2 outlets. Connections are made by using extension cords that have 2 outlets each Find the least number of cords needed to get these computer set up for use. Apply merge sort to the list -1, 0, 2, -2, 3, 6, -3, 5, 1, 4. Find all the spanning trees of the graph shown in Fig.Q.3(c). Also find all the isomorphic spanning trees. Fig.Q.3(c)Obtain an optimal prefix code for the message MISSION SUCCESSFUL. Indicate the code

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- State Krushkal's algorithm. Using Krushkal's algorithm find a minimal spanning tree for the (08 Marks) weighted graph shown in Fig.Q.4(a). Fig.Q.4(a) Apply Dijkstra's algorithm the diagram shown in Fig.Q.4(b) and determine the short Co, Fig.Q.4(b) distance from vertex a to each of the other vertices in the directed graph. c. Define to following with one example for each: Edge connectivity; i) Cut set; (06 Marks) iii) Vertex connectivity. PART - B A bit is either 0 of A byte is a sequence of 8 bits. Find i) The number of bytes; ii) The 5 number of bytes that team with 11 and end 11; iii) the number of bytes that begin with 11 and do not end with 11 (iv) the number of bytes that begin 11 or end with 11. How many arrangements of the letters in MISS SIPPI have no consecutive S's? (05 Marks) b. Find the coefficient of x° in the expansion of $3 | x^2 -$ (05 Marks) apples and 6 oranges among 4 children so that each In how many ways can we distribute child gets at least 1 apple? a. How many integers between and 300 (inclusive 6 i) Divisible by at least one of 5, 6, 8? Define derangement. Find the number of derangements of 1, 2, 3, 4. List all the (06 Marks) derangements. T₁, T₂, T₃, T₄, T₅ are to be made class teachers for five classes, Five teachers C₁, C₂, C₃, C₅ one teacher for each class. T₁ and T₂ do not with to become the class teachers for C1 or C2, T3 and T4 for C4 or C5, and T5 for C3 or C4 or C3 In how many ways (08 Marks) can the teachers be assigned the work? fund the generating function for the sequence 8, 26, 54, 92.... (06 Marks) Using generating function, find the number of i) non negative and ii) positive integer (08 Marks) solutions of the equation $x_1 + x_2 + x_3 + x_4 = 25$. Define exponential generating functions using exponential generating function the number of ways in which 5 of the letters in the word CALCULUS be arranged. (06 Marles The number of bacteria in a culture is 1000 (approximately) and this number increases 250%
 - a. The number of bacteria in a culture is 1000 (approximately) and this number increases 250% every two hours. Use a recurrence relation to determine the number of bacteria present after one day.

 (05 Marks)
 - b. Solve the recurrence relation $a_{n+2} 4a_{n+1} + 3a_n = -200$, $n \ge 0$ and $a_0 = 3000$, $a_1 = 3300$. (07 Marks)
 - c. Find the generating function for the recurrence relation $a_{n+1} a_n = n^2$, $n \ge 0$ and $a_0 = 1$. (08 Marks)